

## ON $r$ -FUZZY WEAKLY $b$ -OPEN FUNCTIONS

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**Abstract.** In this paper, we introduce and characterize a new class of functions called  $r$ -fuzzy weakly  $b$ -open ( $r$ -fuzzy weakly  $b$ -closed) functions between smooth fuzzy topological spaces.

### 1. Introduction and Preliminaries

Functions is a well-known notion in topology. The second author studied various types of functions in Topology [4, 5, 21]. The fuzzy concept has invaded almost all branches of Mathematics since its introduction by Zadeh [23]. Fuzzy sets have applications in many fields such as information [17] and control [20]. The theory of fuzzy topological spaces was introduced and developed by Chang [1] and since then various notions in classical topology have been extended to fuzzy topological spaces. Sostak [18] and Kubiak [10] introduced the fuzzy topology as an extension of Chang's fuzzy topology. It has been developed in many directions. Sostak [19] also published a survey article of the developed areas of fuzzy topological spaces. This paper is organized as follows. In the second section, we provide some background on smooth fuzzy topological spaces and  $r$ -fuzzy sets. We introduce and characterize a new class of functions called  $r$ -fuzzy weakly  $b$ -open ( $r$ -fuzzy weakly  $b$ -closed) functions between smooth fuzzy topological spaces in the third section. Moreover, conclusion and scope for future work were discussed at the end.

### 2. Preliminaries

**Definition 2.1.** A fuzzy point  $x_t$  in  $X$  is a fuzzy set taking value  $t \in I_0$  at  $x$  and zero elsewhere,  $x_t \in \lambda$  if and only if  $t \leq \lambda(x)$ . A fuzzy set  $\lambda$  is quasicoincident with a fuzzy set  $\mu$ , denoted by  $\lambda q \mu$ , if there exists  $x \in X$  such that  $\lambda(x) + \mu(x) > 1$ . Otherwise  $\lambda \bar{q} \mu$ .

**Definition 2.2.** [10, 18] A function  $\tau : I^X \rightarrow I$  is called a smooth fuzzy topology on  $X$  if it satisfies the following conditions:

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