

## DECOMPOSITION OF $(\alpha\text{-}\mathcal{H}_\sigma, \lambda)$ -CONTINUITY

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Date of Receiving : 23. 11. 2022

Date of Revision : 06. 04. 2023

Date of Acceptance : 12. 06. 2023

**Abstract.** In this new research paper we introduce and investigate the new kind of open sets  $\alpha\text{-}\mathcal{H}_\sigma$ -open,  $\sigma\text{-}\mathcal{H}_\sigma$ -open,  $\pi\text{-}\mathcal{H}_\sigma$ -open,  $\beta\text{-}\mathcal{H}_\sigma$ -open sets in hereditary generalized topological spaces. Also, we obtained a decomposition of  $(\alpha\text{-}\mathcal{H}_\sigma, \lambda)$ -continuity and decompositions of  $(\mu, \lambda)$ -continuity.

### 1. Introduction and Preliminaries

In the year 2002, Császár [5] introduced very useful notions of generalized topology and generalized continuity. Consider  $Z$  be a nonempty set and  $\mu$  be a collection from the subsets of  $Z$ . Then  $\mu$  is called a *generalized topology* (briefly GT) if  $\emptyset \in \mu$  and an arbitrary union of elements from  $\mu$  belongs to  $\mu$ . Let  $\mu$  be a generalized topology on  $Z$ , the elements of  $\mu$  are called  $\mu$ -open sets and the complement of  $\mu$ -open sets are called  $\mu$ -closed sets. The generalized-closure of a subset  $A$  of  $X$ , denoted by  $c_\mu(A)$ , is the intersection of all  $\mu$ -closed sets containing  $A$  and the interior of  $A$ , denoted by  $i_\mu(A)$ , is the union of all  $\mu$ -open sets contained in  $A$ . A subset  $L$  of a space  $(Z, \mu)$  is called as  $\mu$ - $\alpha$ -open [6] (resp.  $\mu$ - $\sigma$ -open [6],  $\mu$ - $\pi$ -open [6],  $\mu$ - $\beta$ -open [6]) if  $L \subset i_\mu c_\mu i_\mu(L)$  (resp.  $L \subset c_\mu i_\mu(L)$ ,  $L \subset i_\mu c_\mu(L)$ ,  $L \subset c_\mu i_\mu c_\mu(L)$ ). Let  $Z$  be a space. Then  $\mu(x) = \{U : x \in U \in \mu\}$ . A space  $Z$  is called a  $C_0$ -space [14], if  $C_0 = Z$ , where  $C_0$  is the set of all representative elements of sets of  $\mu$  and  $x$  is called a represent element of  $u \in \mu$  if  $u \subset v$  for each  $v \in \mu(x)$ . A nonempty family  $\mathcal{H}$  of subsets of  $Z$  is called as a *hereditary class* [7], if  $L \in \mathcal{H}$  and  $B \subset L$ , then  $B \in \mathcal{H}$ . For each  $L \subseteq Z$ ,  $L^*(\mathcal{H}, \mu) = \{z \in Z : L \cap V \notin \mathcal{H} \text{ for all } V \in \mu \text{ such that } z \in V\}$ [7]. For  $L \subset Z$ , define  $c_\mu^*(L) = L \cup L^*(\mathcal{H}, \mu)$  and  $\mu^* = \{L \subset Z : Z - L = c_\mu^*(Z - L)\}$ . If  $\mathcal{H}$  is a hereditary class on  $Z$ , then  $(Z, \mu, \mathcal{H})$  is

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2010 *Mathematics Subject Classification.* 54A05.

*Key words and phrases.* hereditary generalized topology,  $\alpha\text{-}\mathcal{H}_\sigma$ -open,  $\sigma\text{-}\mathcal{H}_\sigma$ -open and  $\pi\text{-}\mathcal{H}_\sigma$ -open sets.

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